Spectroscopy of CF₃COZ Compounds. V. Vibrational Spectra and Structure of Solid Trifluoroacetic Acid

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Abstract: Infrared, Raman, and neutron-scattering data are correlated for solid CF₃COOH and CF₃COOD in the region 2000–200 cm⁻¹. Comparisons between liquid and solid CF₃COOH suggest that both phases are composed of hydrogen-bonded chains. Two possible structures are proposed, of which one (monoclinic, P2/m) is favored by the spectroscopic data. Vibrational assignment of CF₃COOH is straightforward, but that of CF₃-COOD is more difficult; the normal modes in the region 910-610 cm⁻¹ apparently change significantly on deuteration. Mixing between the O-D torsion and the O-C-O scissors mode implies a deviation from coplanarity of adjacent carboxyl groups. If this is actually the case, the symmetry of the (rigid) space group is reduced to P2. A solid–solid phase transition is observed at 220.5°K. Raman spectra taken above and below this temperature snow only small frequency differences and suggest that the transition involves a change in the orientation or relative motion of adjacent carboxyl groups.

This series of papers has dealt with vibrational assignments of molecules with the structure $CF_{3}C(=0)Z$, where the Z substituent has been Cl, 28 CF3, 2b H, 3 and F.4 In each case, the attractive forces between the individual molecules of the substance are small, and the material is a gas at room temperature. Although conclusions regarding the equilibrium conformation of $(CF_3)_2C=0$ were drawn from its vibrational spectrum in ref 2b, in most cases the structure of the molecular entity considered has been known from previous microwave⁵ or electron-diffraction⁶ studies.

The subject of the present work is trifluoroacetic acid, CF₃COOH. It is isoelectronic with trifluoroacetyl fluoride, but the redistribution of charges involved in replacing the -F with an -OH group profoundly changes the nature of the intermolecular forces; hydrogen bonds are formed, with the result that CF₃COOH is a liquid at room temperature. It freezes at $-15^{\circ,7}$ and the structure of the resulting solid has not been determined by crystallographic methods. The intimate connection between vibrational properties and structure makes it impossible to discuss the former without assuming a model for the latter. Thus the focus of the present study is on the structure of the material studied to a much larger extent than in the previous works.²⁻⁴

Structure of the Condensed Phases

Clague and Novak⁸ have published a thorough study of the spectra of solid CF₃COOH and CF₃COOD. The lack of correspondence between many of the observed Raman and infrared frequencies led them to conclude that a center of symmetry was present; they further concluded that the solid is thus composed of hydrogenbonded cyclic dimers rather than infinite chains. Formic⁹ and acetic^{10,11} acids contain such hydrogen-

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bonded chains in the solid state, both with space groups of $Pna2_1(C_{2n}^{9})$.

Spectra taken in the course of the present study are in good agreement with those of ref 8, in particular with regard to the differences between the Raman and infrared frequencies. However, the conclusion to be drawn from these differences is not that the solid is associated in the form of dimers, but simply that the unit cell contains a center of symmetry. Two examples of chain structures meeting this requirement are shown in Figure 1. The first is $Pbca(D_{2h}^{15})$; it consists of conventionally linked chains, with molecules in the upper chain related to those in the lower chain by the inversion center (Figure 1a). The basis for a second structure is shown in Figure 1b, with two chains facing each other to form one double chain or ribbon. The carbon and oxygen atoms of each ribbon will be approximately coplanar, and the angle formed by the planes of two adjacent parallel ribbons can be adjusted to satisfy packing requirements, giving a structure of space group $P2/m(C_{2h})$ with four molecules per unit cell.

There is in fact a line of reasoning indicating that CF₃COOH in both the liquid and the solid is associated mainly in the form of chains. (a) The dielectric constant¹² of liquid CF₃COOH at 20° is 39.5. This is a very high value compared with that of $CH_{3}COOH(6.15)$, which consists mostly of dimers in the liquid phase, but it is comparable with that of HCOOH (58.5), which is known to form chains.13 The dielectric constant of CF₃COOH changes by almost a factor of 2 on going from -11 to 28° ,¹⁴ an observation which is easily explained if the liquid is composed of chains (whose average length would depend on the temperature), but is anomalous if the liquid is composed of dimers. In addition, Murty and Pitzer¹⁵ have studied the infrared

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Figure 1. Possible chain structures for solid CF₃COOH. (a) Pbca ($D_{2\lambda}$ ¹⁵). Monomers in the upper chain are related to those in the lower chain by the inversion operation (asterisk). The unit cell contains two monomers (comprising a catemer) from each of the two chains. Hydrogen bonds are indicated by dashed lines. (b) P2/m ($C_{2\lambda}$ ¹). The inversion relates monomers facing each other in the double chain, so that the catemer is structurally similar to the gas-phase dimer. The unit cell contains a catemer from the pictured chain (enclosed by dash-dotted lines) plus one from another chain parallel to it, but with the plane oriented at an angle determined by packing requirements. Spectroscopic evidence discussed in the text supports this model.

spectra of trifluoroacetic acid in nonpolar solvents and concluded that the association is primarily linear. (b) Neutron-scattering spectra of CF₃COOH have been obtained for both the liquid and the solid (Figure 2). The inelastic-scattering features (channels below ~ 160) stay remarkably constant over the phase change. Thus if the liquid consists of hydrogen-bonded chains, the solid must be similarly constructed.

Both of the structures under consideration (Figure 1) have unit cells containing four monomers, two each from neighboring chains. Adjacent monomers in a given chain are obviously more closely coupled than monomers in neighboring chains, and it will be convenient to have a specific term for such a vibrational entity. We suggest *catemer* (Latin *catena*, chain), which can be generally defined as that sequence of monomers in a chain which are related by symmetry elements other than simple translation. The factor group of the catemer in the *Pbca* (orthorhombic) struc-



Figure 2. Neutron inelastic-scattering spectra of CF₃COOH. Wave number equivalents of some of the channels are indicated (458..., 27 cm⁻¹). Intense Bragg peaks are observed in the solid for neutron wavelengths of 5.23 and 5.55 Å; they can be interpreted as the 100 and 002 reflections of a monoclinic unit cell with parameters a = 5.25, b = 9.165, c = 11.142 Å, and $\beta = 85^{\circ}$.

ture is C_{2v} and the representation of the internal vibrations is

$$\Gamma_{\rm int}(C_{2v}) = 12a_1 + 6a_2 + 12b_1 + 6b_2$$

where the a_1 , b_1 , and b_2 vibrations are infrared active and all the vibrations are Raman active. If the monomer is regarded as belonging to the point group C_s , the *Pbca* model predicts that all modes in the solid originating as a' vibrations in the monomer will be split by catemeric coupling in the infrared and that all modes will be split in the Raman.

In the P2/m (monoclinic) model, the factor group of the catemer is C_{2h} , and the representation of the internal vibrations is

$$\Gamma_{\rm int}(C_{2\hbar}) = 12a_{\rm g} + 6b_{\rm g} + 6a_{\rm u} + 12b_{\rm u}$$

In this case, the principle of mutual exclusion holds within the catemer; in-phase vibrations of the two monomers are a_g or b_g and Raman active, while out-ofphase modes are a_u or b_u and infrared-active. The only splitting observed using this model will be due to interchain coupling.

With the exception of the O-H(D) stretches and CF₃ torsions, all of the internal vibrations of CF₃COOH and CF₃COOD are found between 1900 and 200 cm⁻¹. Spectra for these two species are given in Figures 3 and 4. Although evaluation of the amount of splitting present is complicated by numerous instances of Fermi resonance, it is clear that the overall pattern is more in accord with $\Gamma_{int}(C_{2h})$ than with $\Gamma_{int}(C_{2v})$. In particular, the large difference between the position of the C==O stretch in the Raman (1706 cm⁻¹) and the infrared (1763 cm⁻¹) suggests a catemeric center of symmetry, as does the lack of splitting in most of the sharp peaks.





Figure 3. Spectra of solid CF₃COOH. (a) Neutron inelastic-scattering spectrum. Data of Collins and Haywood¹⁹ are plotted with black dots (ordinate represents percentage of monitor counts). Diamond-shaped points are the data of Figure 2b, linearly scaled to match at 398 cm⁻¹. (b) Raman spectrum. (c) Infrared spectrum.



Figure 4. Spectra of solid CF_3COOD . (a) Raman spectrum. (b) Infrared spectrum. Peaks due to CF_3COOH are indicated by a dashed line.

Thus the P2/m structure is favored by the spectroscopic evidence and will be assumed to be correct throughout the rest of this paper. In this case, the catemer is

structurally similar to the cyclic dimer found in the gas phase. The present study is thus in essential agreement with the spectroscopic analysis given by Clague and Novak.⁸ differing mainly in that their use of the term dimer seems to exclude a chain structure.

The P2/m model illustrated in Figure 1b has equal distances between the carbonyl and hydroxyl oxygen atoms in the same catemer and those in adjacent catemers; this is a result of the assumed spherical nature of the van der Waals potential surfaces rather than the presence of any formal symmetry element. It suggests that the hydrogen bonds in solid CF₃COOH may be bifurcated, a situation which is unusual but not unprecedented.¹⁶ It would be interesting to have definitive results (e.g., from a neutron-diffraction investigation) to clear up this point.

Experimental Section

The spectra displayed in Figure 2 were obtained on a time of flight spectrometer at the Army Materials and Mechanics Research Center, Watertown, Mass.; this type of instrument has been pre-viously described in the literature.^{17,18} Figure 3a shows neutronscattering data obtained by Collins and Haywood¹⁹ using a spectrometer measuring energy loss rather than energy gain. This instrument extends the useful range of observation to $\sim 1400 \text{ cm}^{-1}$ or more, providing much more information on the internal modes of the molecule and allowing more detailed comparison with the Raman and infrared spectra

Raman spectra of CF₃COOH (Figure 3b) and CF₃COOD (Figure 4a) were run using the 5145-Å line of an Ar⁺ laser at \sim 600 mW and a Spex monochromator.²⁰ The samples were placed in glass tubes and mounted in an unsilvered Dewar which was then cooled with boil-off from a supply of liquid nitrogen. The temperature of the solid was not closely controlled and ranged from 258 °K (the freezing point) to about 210°K. The spectra were calibrated with Ar emission lines.21,22

A conventional liquid-nitrogen cold cell²³ was used in running the infrared spectra (Figures 3c and 4b). Both outer windows and the cold window were CsI. ' Samples were deposited from the vapor state and annealed by repeated warming and recooling. The temperature of the sample as the spectra were run was about 106°K. Calibration was carried out using the absorption lines of atmospheric water vapor.²⁴ The instrument used was a Beckman IR-12. Resolution and frequency accuracy for the optical spectra reported here are within 2 cm⁻¹.

The CF₃COOH used in the Raman experiments was obtained from Pierce Chemical, Rockford, Ill., and was labeled "99+% pure." The CF3COOD was from Bio-Rad Laboratories, Richmond, Calif.; the isotopic composition was given as 99 atom % D. Samples used in the infrared experiments were from Eastman Organic Chemicals, Rochester, N. Y., and an older specimen of CF3COOD from Bio-Rad labeled 98 atom % D. Additional infrared experiments with mixtures of varying isotopic composition were carried out to identify features due to CF₃COOH in CF₃COOD,

A differential thermal analysis experiment was carried out on CF₃COOH using a Du Pont Model 900 instrument equipped with a differential scanning calorimeter cell. The sample was initially cooled to 173 °K with liquid nitrogen and then was heated at 5 °/min. Two endothermic peaks were found, a weak one at 220.5°K and a strong one at 257.9 °K. The latter corresponds to melting of the sample, so the former must represent a solid-solid phase transition. This observation immediately raises the question of whether the Raman spectra of Figures 3b and 4a (for the most part taken above 220°K) can properly be compared with the infrared spectra of Figures 3c and 4b (taken at ~ 106 °K). Fortunately, the Raman spectra of ref 8 were taken at \sim 77 °K, and the agreement between the two sets of observations indicates that the comparison remains valid. Frequency differences average less than 2 cm⁻¹, well within the combined error limits. The largest discrepancies occur for v_{C-0} (1475 vs. 1482⁸ for CF₃COOH, 1439 vs. 1444⁸ for CF₃COOD) and for δ_{COH} (1324 vs. 1330⁸ and 1073 vs. 1076⁸).

Vibrational Assignment

CF₃COOH. Assignments for the fundamental frequencies of solid CF₃COOH are given in Table I, together

Table I.	Fundamental Frequencies of CF ₃ COOH
(Cyclic D	imer and Solid)

	Cyclic dimer ^a	Solid	
Description	Ir, Ne matrix	Ir	Raman
νon	2922	2918	
$\nu_{C=O}$	1786	1763	1706
$\nu_{\rm C-O}$	1475	1477	1475
δ _{COH}	1318	1314	1324
		1309	
$\nu_{\rm FCF}$	1244	1225	1231
VFCF	1197	1196	1210
VCF3	1178	1182	1182
•		1171	
$ au_{ m OH}$	927	904	[~875]°
•		891	•
νcc	828	830	816
δ_{CF_3}	686	775	781
δοςο	712	717	701
$\delta_{\rm FCF}$	607 ^b	609	598
δ_{FCF}	520 ^b	520	524
Wantigear	459	460	439
Pantigear	390	402	423
ωgear	240	301	272
ρ_{gear}	240	258	267
$ au_{\mathrm{CF}_3}$		[∼27 ?]°	[∼27?]°

^a Table 4, ref 25. ^b Interchanged from Table 4, ref 25, but in agreement with the text. ^c From neutron-scattering measurements.

with infrared frequencies for the cyclic dimers from the matrix-isolation work of Redington and Lin.25 The descriptive notation follows the usage of ref 4 and 25. Particularly above 1000 cm⁻¹, there is a close correspondence between the frequencies of the solid and dimer; since clear arguments for the assignment of $\nu_{C=0}$, $\nu_{C=0}$, δ_{COH} , and the C-F stretching vibrations are given in ref 8 and 25, they will not be repeated here.

Consideration of neutron-scattering data in conjunction with infrared and Raman spectra can lead to a considerable increase in the certainty of the analysis since the neutron scattering is especially sensitive to motions of ¹H nuclei.²⁶ Figure 3a depicts the neutronscattering spectrum of CF₃COOH as observed by Collins and Haywood,19 with additional data from experiments carried out by the present author. The spectrum is dominated by the intense doublet around 900 cm^{-1} , which must be the torsional motion of the hydroxyl group, τ_{OH} . The splitting is probably due to frequency differences between the gerade and ungerade modes, since the lower-frequency peak (\sim 875 cm⁻¹) is below the corresponding infrared feature (904, 891 cm⁻¹). The splitting in the infrared must be due to interchain

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Infrared ^a			man	····
		A.,	Rel neak	
cm ⁻¹	Inten	cm^{-1}	height	Assignment ^b
~ 1860	VW			
1834	vw			$\nu^{g}_{FCF_{2}} + \delta^{u}_{FCF_{2}} (1231 + 609 = 1840)$
1786 sh	w			$\delta^{g}_{COH} + \omega^{u}_{antigear} (1324 + 460 = 1784)$
1774 sh	W			$\nu^{g}_{C,0} + \omega^{u}_{max} (1475 + 301 = 1776)$
1763	VC			
1765	v 3			V = 0 (1021 + 500 - 1751)
1750	m			$\nu^{e}_{FCF_{2}} + o^{e}_{FCF} (1231 + 520 = 1/51)$
1733	W			
1722	W			
		\sim 1720 sh	\sim 3	$\delta^{u}_{COH} + \rho^{u}_{antigent} (1309 + 402 = 1711)$
		1706	7	
		a 1690 ch	- 1	$y_{n-1} = \frac{1}{2} \frac{3n}{2} \frac{1}{2} \frac$
1 600		×1090 SII	/~4	$\nu_{\rm CF_3} + \nu_{\rm FCF} (1102 + 324 = 1700)$
1680	mw			$\nu^{\rm g}_{\rm FCF_2} + \omega^{\rm u}_{\rm antigear} (1231 + 460 = 1691)$
1627	mw			$\nu^{g}_{FCF_{2}} + \rho^{u}_{antigear} (1231 + 402 = 1633)$
~1590	vw			$\delta^{g}_{OCO} + \tau^{u}_{OH} (701 + 904 = 1605)$
1553	m			$\delta^{g}_{CE} + \delta^{u}_{CE} (781 + 775 = 1556)$
1477	e			
1477	3	1475	14	
4.422		1475	14	ν°C-0
1432	vw		_	$\nu^{\rm g}_{\rm CF_3} + \rho^{\rm u}_{\rm gear} (1182 + 258 = 1440)$
		1324	5	δ ^g COH
1314)				\$11
1309	S			0"COH
1296 sh	337			
1290 \$11	vv	1001	2	
		1231	3	ν ^e FCF ₂
1225	VS			ν^{u} FCF ₂
		1210	3	ν ^g FCF
1208	w			$\delta^{g}_{FCF_{a}} + \delta^{u}_{FCF_{a}} (598 + 609 = 1207)$
1196	m			V ^u FCF
1120		1182	0	· FCF
		1182	0	$V^{\circ}CF_{3}$
		1170	6	$\delta^{u}_{CF_{3}} + \rho^{u}_{antigear} (7.5 + 402 = 1177)$
1182	Ve			$\nu^{\rm u} {\rm CF}_{\rm s}$
1171 (•5			$\delta^{g}_{CF_{3}} + \rho^{u}_{antigear} (781 + 402 = 1183)$
1156	w			$\nu_{\rm CF}$ (CF ₃ ¹³ COOH)
1149	W			$\mu_{\rm CP}$ (13CF COOH)
904	**			
904	S			$ au_{ m OH}$
891)				
880 sh				
842	m			$\omega^{g}_{antigear} + \rho^{u}_{antigear} (439 + 402 = 841)$
830	ms			ν ^u cc
820	m			$\rho_{gastimus}^{g} + \rho_{astisus}^{u} (423 + 402 = 825)$
020		816	100	p antigear (p antigear (20 102 020)
		706	100	$\nu^{-}CC$
		/90	9	$2\rho^{a}_{antigear} (2 \times 402 = 804)$
		781	6	$\delta^{g}_{CF_{3}}$
775	m			$\delta^{u}_{CF_{a}}$
717	S			δ ^u oco
		711	2	$\omega^{g}_{anti-ant} + \omega^{g}_{ant} (439 + 271 = 710)$
		701	õ	Source and the second s
		701	3	
		695	6	$\partial^{\mathbf{g}}_{\text{antigear}} + \omega^{\mathbf{g}}_{\text{gear}} (423 + 271 = 694)$
609	m			$\delta^{u}_{FCF_{2}}$
		598	14	δ^{g}_{FCF}
		528 sh	2	$2\rho^{g}_{max}$ (2 × 267 = 534)
		524		
520		524	5	5°FCF
520	111			OUFCF
460	ms	100		$\omega^{\mathtt{u}}_{\mathrm{antigear}}$
		439	33	$\omega^{g}_{antigear}$
		423	30	$\rho^{g}_{antigear}$
402	m			$\rho^{\rm u}_{\rm antigear}$
301	ms			() ^u mor
201	1113	271	22	∽ gear
		2/1	23	w ⁻ gear
		207 sh	\sim 12	$ ho^{s}_{gear}$
258	m			$ ho^{\mathrm{u}}_{\mathrm{gear}}$

Table II. Infrared and Raman Spectra of Solid CF₃COOH (2000-200 cm⁻¹)

a sh = shoulder; v, w, m, s = very, weak, medium, strong. b In many cases, more than one combination is available to explain a given peak. To save space, only one of the possibilities (usually chosen on the basis of likelihood of coupling) is given here.

coupling, since all ir-active modes are ungerade. With the possible exception of ν_{CF_3} (for which an alternate explanation in terms of Fermi-resonant combinations is available), the only modes which exhibit interchain coupling are those which involve large-amplitude motions of the hydrogen atom.

carboxyl group. The presence of a moderately strong peak in the neutron-scattering spectrum around 700 cm⁻¹ leads to the association of this mode with the Raman peak at 701 cm⁻¹ and the strong infrared peak at 717 cm⁻¹.

Another vibrational mode which must involve the hydrogen atom is δ_{oCO} , the scissors deformation of the

The carbon-carbon stretching mode (strongly coupled with the symmetric C-F stretching vibration) is easily identified by its intensity in the Raman spectrum (Figure 3b). The corresponding infrared feature is a distinctive triplet (842, 830, 820 cm⁻¹) in which the outer members can be assigned to combinations (Table II). The only other fundamental expected to fall in this region is the trifluoromethyl umbrella deformation, δ_{CF_i} . This is evidently the sharp peak at 775 cm⁻¹ in the infrared. If it is identified with the 781-cm⁻¹ feature in the Raman spectrum, the 796-cm⁻¹ peak can be explained as the overtone of the 402-cm⁻¹ mode. This assignment puts $\delta_{CF_{3}}$ abve δ_{OCO} , contrary to the corresponding assignments for CF₃CFO⁴ ($\delta_{OCF} = 761$, $\delta_{CF_3} = 692$ cm⁻¹), for monomeric CF₃COOH²⁵ ($\delta_{OCO} = 781$, $\delta_{CF_3} = 663$ cm⁻¹) and, to a smaller extent, for the ungerade vibrations of the dimer²⁵ ($\delta_{OCO} = 712$, $\delta_{CF_3} = 686$ cm⁻¹). The reduction of the separation between the two modes (from 118 to 26 cm^{-1}) as the dimer is formed shows that these vibrations (especially δ_{OCO}) are association-sensitive; since the solid is even more strongly associated than the dimer, further changes in position are not unreasonable. It should also be noted that the modes labeled ν_{CF_3} , ν_{CC} , δ_{OCO} , and δ_{CF_3} all imply a large component of motion along the C-C bond and thus will all interact strongly. The actual normal coordinates may differ widely from compound to compound.

The other assignments in the 700–200 cm⁻¹ region follow readily from comparison with other CF₃COZ molecules.^{3,4} The similarity between CF₃COOH and CF₃CFO⁴ with regard to frequencies and relative intensities in both the Raman and the infrared is particularly striking.

CF₃**COOD.** The incoherent scattering cross section of the deuteron is an order of magnitude smaller than that of the proton, and the neutron scattering of CF₃-COOD has not been studied. Thus our main tool in analyzing the Raman and infrared spectra of CF₃COOD (Figure 4) will be comparison with CF₃COOH. Except for the movement of δ_{COH} from 1324 to 1073 cm⁻¹, the pattern of Raman-active vibrations is virtually unchanged on deuteration. Accordingly, we assign peaks at 800, 782, 658, and 597 cm⁻¹ to ν^{g}_{CO} , $\delta^{g}_{CF_{3}}$, δ^{g}_{OCO} , and $\delta^{g}_{FCF_{2}}$ (where the superscript g is used to distinguish the gerade mode of the catemer from its infrared-active counterpart).

Most of the absorptions in the infrared spectrum (Figure 4b) are also easily assigned. The C-F stretching region ($1250-1150 \text{ cm}^{-1}$) is almost exactly the same as for CF₃COOH. The peak at 1037 cm⁻¹ is obviously the COD deformation. Below 610 cm⁻¹ we again have a pattern virtually identical to that found in CF₃COOH, and the same assignments can be made (Table III). It is in the region 910-610 cm⁻¹ that the pattern changes drastically and a firm assignment becomes correspondingly difficult.

The four fundamentals expected to occur in this region are ν_{CC} , τ_{OD} , δ_{CF_3} , and δ_{OCO} (superscript u understood). The first of these can be identified with the doublet at 825, 816 cm⁻¹ [where the doubling is explained as Fermi resonance with $\delta^{g}_{FCF} + \omega^{u}_{gear}$ (523 + 285 = 818) or $\rho^{g}_{antigear} + \rho^{u}_{antigear}$ (417 + 397 = 814)]. The sharp, weak peaks at 785 and 778 cm⁻¹ have plausible explanations as combinations (Table IV), so we now have three fundamental modes to distribute among the four major features (801–793, 711, 690, and 647 cm⁻¹) in this region.

The 690- and 647-cm⁻¹ peaks are of equivalent width

Table III. Fundamental Frequencies of CF₈COOD (Cyclic Dimer and Solid)

	Cvclic dimer ^a		Solid
Description	Ir, Ar matrix	Ir	Raman
ν _{OD}	2254	2241	2052
$\nu_{\rm C=0}$	1780	1767	1690
$\nu_{C=O}$	1435	1443	1439
$\nu_{\rm FCF_2}$	1243	1223	1230
$\nu_{\rm FCF}$	1192	1205	1211
$\nu_{\rm CF_3}$	1178	1192	1181
		1181	
$\delta_{\rm COD}$	1042	1037	1073
νcc	817	825	800
δ_{CF_3}	682	711	782
δοςο	706	801	658
		793	
$ au_{ m OD}$	800	690	
		647	
δ_{FCF} .	603 ^b	605	597
δ_{FCF}	502 ^b	516	523
Wantigear	455	456	439
$\rho_{\rm antigear}$	[39 0]¢	397	417
ω_{gear}	[240] ^c	295	272
$\rho_{\rm gear}$	[240] ^c	254	267

^a Table 4, ref 25. ^b Interchanged from Table 4, ref 25, but in agreement with the text. ^c (CF₃COOH)₂ value.

and intensity, and the natural way to make the number of modes and features come out even is to attribute these two peaks to the same fundamental, split either by Fermi resonance or by an unusual amount of interchain coupling. All possible assignments in this region can now be described by the six permutations of the symbols (τ_{OD} , δ_{CF} , δ_{OCO}) or (1 2 3).

The most straightforward assignment is the one designated (1 2 3) above. The 801, 793 cm⁻¹ feature is similar in intensity and appearance to τ_{OH} (904, 891) in CF₃COOH, though not so broad. The 711-cm⁻¹ peak is as narrow as δ_{CF_4} (775) in CF₃COOH, though more intense. The intensity of each component of the 690, 647 doublet is similar to that of δ_{OCO} (717) in CF₃COOH. However, there is one major objection to this assignment: it implies a frequency ratio τ_{OH}/τ_{OD} of 1.14, much smaller than the value of 1.3–1.4 expected for this quantity. In addition, it raises the questions of why the δ_{OCO} mode is split so grossly in CF₃COOD and not in CF₃COOH and why $\delta^{\mathbf{g}}_{CF_3} - \delta^{\mathbf{u}}_{CF_3}$ increases from 6 to 71 cm⁻¹ on deuteration. It will evidently be worth our while to examine the other assignments.

(1 3 2) parallels the frequency order of the assignment made by Redington and Lin^{25} for cyclic CF₃COOD dimers, but it requires us to believe that the mode producing the sharp, moderately weak singlet at 775 cm⁻¹ in CF₃COOH gives rise to the broad, intense doublet at 690, 647 cm⁻¹ in CF₃COOD, and can thus be rejected. Assignments (2 1 3) and (3 1 2) both identify the sharp singlet at 711 cm⁻¹ as τ_{OD} , which again strains credulity.

We are now left with (2 3 1) and (3 2 1). Both assign the 690, 647 doublet as τ_{OD} , giving an isotopic frequency ratio of 1.35, in the middle of the expected range. Since τ_{OD} probably involves the largest amplitudes of any of the three vibrations being considered, these assignments ease the burden of explaining the gross splitting. (Even if Fermi resonance is invoked, large anharmonic terms in the potential function are required to produce the amount of mixing observed.) The former assignment minimizes $\delta^{z}_{CF_{z}} - \delta^{u}_{CF_{z}}$ and $\delta^{z}_{OCO} - \delta^{u}_{OCO}$ but is

714	
Table IV.	Infrared and Raman Spectra of Solid CF ₃ COOD (2000–200 cm ⁻¹)

Infrare	da	Ra	man	
	Tutan	A am=1	Del neels ht	Accianmonth
ν , cm -	inten	$\Delta \nu$, cm -	Rei peak in	Assignment
1007				
1987	vw			$\nu^{g}_{CC} + \nu^{u}_{CF_{3}}(800 + 1192 = 1992)$
1882	vw			$\omega^{g_{antigen}} + \nu^{u}_{CO} (439 + 1443 = 1882)$
1863	¥75¥7			$(417 \pm 1/43 - 1860)$
1005	* **			$p^{-antigear} + v^{-}C = 0 (417 + 1443 = 1000)$
1839	vw			$\nu^{g}_{CC} + \delta^{u}_{COD} (800 + 1037 = 1837)$
1819	vw			$\delta^{g}_{CF_{a}} + \delta^{u}_{COD} (782 + 1037 = 1819)$
a 1777 sh	337			$\delta f_{\text{Rgp}} + v = (597 + 1187 - 1784)$
	vv			$\nu_{\rm FCF_2} + \nu_{\rm CF_3} (337 + 1187 = 1784)$
1767	vs			ν^{u} C=O
1758	s			$\delta^{g}_{COD} + [690] (1073 + 690 = 1763)$
~ 1714 sh				$y_{max} \pm \delta_{max} (1230 \pm 516 - 1223 \pm 523)$
1700	**			$PFCF_2 + 0FCF(1230 + 510 - 1223 + 523)$
1/22	w			$\nu_{\rm C-0} + \omega^{\rm u}_{\rm gear} (1439 + 295 = 1734)$
1699	mw			$\rho^{g}_{gear} + \nu^{u}_{C-O} (267 + 1433 = 1710)$
		1690	11	ν ⁸ C_0
1571	\$1557			1181 + 207 - 1578
1571	• • •			$p^{2}CF_{3} + p^{2}$ antigear (1101 + 597 - 1578)
1552	vw			$\delta^{g}_{FCF} + \delta_{COD} (523 + 1037 = 1560)$
1483	mw			$\nu_{\rm C-O}$ (CF ₃ COOH)
1443	5			N ^U O O
1445	3	1 4 2 0		
		1439	6	ν ^ε C-0
		1428 sh	~ 4	$\delta^{u}_{COD} + \rho^{u}_{antigear} (1037 + 397 = 1434)$
1405	VW			$\mu_{000}^{\mu} + \delta_{\mu_{000}}^{\mu} = (800 + 605 = 1405)$
1 205				$r_{1} = r_{1} = r_{1} = r_{2} = r_{1} = r_{2} = r_{1} = r_{2} = r_{2} = r_{1} = r_{2} = r_{1} = r_{2} = r_{1} = r_{1} = r_{2} = r_{1} = r_{1$
1385	w			$0^{6} \text{FCF}_{2} + 0^{6} \text{OCO} (397 + 793 = 1390)$
1351	vw			$\delta^{g}_{FCF} + \nu^{u}_{CC} (523 + 825 = 1348)$
1323	mw			δcow (CF ₂ COOH)
1214				
1314	vw			$0^{\circ}COH (CF_3CUUH)_2$
		1237	1	$\nu^{g}_{CC} + \omega^{g}_{antigear} (800 + 439 = 1239)$
		1230	2	VERCE
1 2 2 3	16	1220	-	
1223	VS			^p ⁻ FCF ₂
1212 sh	w			$\rho^{g}_{antigear} + \delta^{u}_{OCO} (417 + 793 = 1210)$
		1211	3	ν ^g FCF
1205	m			Numan .
1205	111			VFCF
1192	VS			N ^L OD
1181	*3			V CF3
1173 sh				
1175 311		1101	10	
		1181	12	ν ^g CF _a
1159	w			$\nu_{\rm CF_2}$ (CF ₃ ¹³ COOD)
1151	W			
1101	••	1072	10	
		1073	10	0°COD
		1053	1	$\omega^{u_{antigear}} + \delta^{u_{FCF_{a}}} (456 + 605 = 1061)$
1054	m			$\delta 8_{000} \pm 0^{4} + (658 \pm 397 = 1055)$
1037				b = 0.00 + p antigear (0.00 + 0.01 - 10.00)
1037	S			0 ⁴ COD
1027	vw			
902	w			
007)				
002	m			τ_{OH} (CF ₂ COOH)
876				· on (• • • • • • • • • • • • • • • • • •
825	mw	8210	3	^{vu} cc
916		9146	ž	(417 + 307 - 914)
810	11100	814		0° antigear $\pm p^{\circ}$ antigear (417 $\pm 597 = 614$)
		800	70	ν ^g cc
		792 sh	~12	$2\rho^{u_{antimear}} (2 \times 397 = 794)$
		780	21	SP
201)		762	21	0°CF3
801 (e			84aaa
793	3			0.00
785 [´] sh	33/			$\omega_{\text{max}}^{\text{s}} + \delta_{\text{max}}^{\text{u}} (272 + 516 = 788)$
770	**			$= \frac{1}{2} \exp \left(\frac$
//8	w			$\rho_{\text{gear}} + o_{\text{FCF}}^{\text{u}}(207 + 510 = 785)$
768	vw			$\delta^{g}_{FCF} + \rho^{u}_{gear} (523 + 254 = 777)$
716 sh	vw	708	1	δoco (CF ₂ COOH)
711			1	\$u _
/11	IIIS			0°CFa
690	S			$\omega^{g}_{gear} + \rho^{u}_{antigear} (272 + 397 = 669) \text{ in}$
				resonance with τ_{OD}
6710				
0/4	111w			
		6/1	3	
		663	~ 18	
		658	12	(Beaco
6.47		050	12	
04/	S			$\tau_{\rm OD}$ in resonance with $\omega^{\rm g}_{\rm gear} + \rho^{\rm u}_{\rm antigear}$
605	ms			$\delta^{u}_{FCF_{2}}$
		597	12	ÅSTOT.
		577	12	
		323	4	0°FCF
516	m			$\delta^{\mathrm{u}}_{\mathrm{FCF}}$
456	s			(J) ^U antiman
	2	120	41	arrentigout
		+37	41	w ^{ant} igear
-		417	30	ρ ^g antigear
397	m			0 ^u antigear
295	s			, univigues
<i>290</i>	3	27.2	10	w_gear
		212	18	$\omega^{\mathbf{g}}_{\mathbf{gear}}$
		267	17	0 ^g gear
254	m			∩"
20 T				

^a sh = shoulder; v, w, m, s = very, weak, medium, strong. ^b Assignment (3 2 1) in the region 910-610 cm⁻¹ is used here for convenience. See text, p 713. ^c Vibration due to mixed catemer (CF₃COOD·CF₃COOH). Journal of the American Chemical Society | 95:3 | February 7, 1973 difficult to rationalize with regard to shapes and intensities, while the latter, (3 2 1), does the opposite.

We are left with the feeling that none of the proposed assignments can by itself give a completely satisfactory account of the observed spectrum. Evidently deuteration induces a considerable redistribution of internal coordinates among the normal coordinates of all three vibrations in this region. This conclusion is particularly interesting in that it implies mixing between τ_{OD} and δ_{OCO} , which could not occur if the catemer contained a plane of symmetry.

Redington and Lin²⁵ have concluded that the CF₃ group in the matrix-isolated CF₃COOH momomer is twisted by perhaps 10-20° out of the skeletal plane. This twist formally changes the point group from C_s to C_1 , but it seems insufficient to account for significant coupling between $\tau_{\rm OD}$ and $\delta_{\rm OCO}$ in the solid, since the CF₃ group retains approximate local threefold symmetry and is thus dynamically isotropic, as well as being physically distant from the carboxyl group. A more direct coupling between the torsion and the scissors mode would arise if the two carboxyl groups within the catemer were not strictly coplanar, but were overlapped or puckered in the manner suggested in Figure 1b. This change nominally reduces the catemeric factor group to C_2 and the space group to P2 (monoclinic), but the distortion from P2/m need not be large. In addition, the barrier separating a carbonyl/hydroxyl overlap from its inverse (hydroxyl/carbonyl) should be no more than a couple of hundred reciprocal centimeters, so that a nonrigid space group isomorphic with P2/m would provide a more appropriate description for this structure than P2.

This example of an additional element of symmetry being provided by a low-energy structural adjustment leads us to inquire whether there are any others available to this substance. The answer is a qualified yes: if a number of protons are cooperatively transferred from their hydroxyl oxygens to the carbonyl oxygens of the next unit cell (e.g., from left to right in the top row of Figure 1b, from right to left in the bottom row) and electrons, skeletal atoms, and CF₃ groups are allowed to relax, a chain will result which is merely the original structure reflected in a plane normal to the chain axis. The nonrigid space group which includes this operation will be isomorphic with $P2_1/m$. The barrier for this operation is hard to estimate offhand, but it should certainly be no lower than the 1700 cm⁻¹ hypothesized for a similar transfer within the CF₃COOH monomer.²⁵ Thus (if O/O overlapping is indeed present) the structure of solid $CF_{3}COOH$ can be represented by a hierarchy of symmetry groups whose individual contributions will depend on the energy available to the system.

$$P2 \xrightarrow[barrier < 1 \text{ kcal/mol}]{} P2/m \xrightarrow[barrier > 5 \text{ kcal/mol}]{} P2_1/m$$

Since the temperature at which $kT/hc = 1700 \text{ cm}^{-1}$ is around 2500°K, the extension to $P2_1/m$ will be unimportant except as a limiting case for techniques such as X-ray diffraction, where the position of the proton and the distinction between a carbonyl and a hydroxyl oxygen are not dominant. The temperature for which kT/hc is, say 150 cm⁻¹, however, is only 216°K, well below the melting point (258°K). It is thus possible that the phase transition a: 220.5°K reported above represents the elimination of O/O overlap (the onset of free puckering), though of course other explanations (e.g., the onset of free rotation of the CF₃ group) are available. The fact that the largest frequency differences over the phase change involve ν_{C-0} and δ_{COH} tends to support hypotheses involving the carboxyl groups.

Conclusions

(1) Neutron-scattering studies of liquid and solid CF₃COOH reported in the present work, considered in conjunction with earlier dielectric-constant^{12,14} and spectroscopic^{13,15} studies, indicate that this substance (in both states) is associated primarily in the form of hydrogen-bonded chains.

(2) Frequency differences between the infrared and Raman spectra of the solid indicate the presence of a center of symmetry in the unit cell. Of two simple structural models incorporating chains and a center of symmetry, one (monoclinic, P2/m) satisfactorily accommodates all experimental data presently available. The structural feature basic to this model is a double chain; its geometry suggests the presence of bifurcated hydrogen bonds.¹⁶

(3) Vibrational assignments for CF₃COOH and CF₃COOD in the region 2000–200 cm⁻¹ are presented in Tables II and IV. Infrared, Raman, and neutron-scattering data¹⁹ have been considered simultaneously in making the assignments, as have results from closely related molecules.^{3,4} Observed interactions between vibrations which could not interact if the catemeric unit had a plane of symmetry suggest that such a plane is absent. A puckering of the catemeric unit about the carboxyl groups may be the rea on. This change formally reduces the space group to P2.

(4) Evidence has been found for the existence of a solid-solid phase transition in CF_3COOH at 220.5°K. Spectroscopic data suggest that the rearrangement involves the carboxyl groups. Definitive results on the structure of the solid and the nature of the transition cannot be obtained spectroscopically, of course, and will be available only after the necessary diffraction studies have been carried out.

(5) The region 910-610 cm^{-1} in the infrared spectrum of CF₃COOD is difficult to interpret, and evidently involves a change in the nature of the normal modes compared with CF₃COOH. This may or may not involve a change in the potential function around the hydroxyl group on deuteration (a normal-coordinate analysis must be carried out before even a tentative answer to this question can be obtained). Taylor and Templeton's observation²⁷ of different heats of dissociation for the deuterated and undeuterated gas-phase dimers indicates that a change in the potential function may well occur. In addition, Costain and Srivastava²⁸ found significant differences in the $O \cdots O$ distances of deuterated and undeuterated bimolecules formed from trifluoroacetic and formic acid. Spectroscopic studies of chromous acid²⁹ and monomeric acetic acid³⁰ have provided evidence for changes in the potential functions on deuteration of these compounds.

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Electronic and Electron Spin Resonance Spectroscopic Study of the Sensitized Decomposition of Formaldehyde

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Abstract: The sensitized decomposition of formaldehyde to formyl radical was examined using triphenylamine (TPA) and primarily in dichloromethane, in 3-methylpentane, and on silica gel at 77° K. The formation of formyl radical is monophotonic in dichloromethane and primarily biphotonic in 3-methylpentane and on silica gel. We propose (1) the monophotonic process occurs *via* energy transfer from the first excited singlet state of TPA and an excimer or exciplex may be involved and (2), the biphotonic process occurs *via* energy transfer from an upper excited triplet state, T₂ or greater, of TPA and an excimer or exciplex may be involved. Another mechanism could also exist in these cases. The disappearance of formyl radical apparently occurs *via* both second- and first-order processes. A solvent radical of dichloromethane is produced in the presence of formaldehyde and a mechanism is proposed for its formation.

The absorption spectrum of formyl radical in the visible region has been detected by Herzberg and Ramsay¹ in the flash photolysis of acetaldehyde in the gas phase. Pimentel, *et al.*,² studied the infrared absorption spectrum of formyl radical, obtained by the photolysis of HI in CO at 20°K. From the same method of obtaining the formyl radical, Adrian and Cochran^{3.4} studied the esr spectrum. Marx and Chachaty³ obtained the formyl radical by γ , X, and uv irradiation of solid formaldehyde at 77°K. Other methods have been used as the irradiation of watermethanol solutions at 77°K⁶ or crystals of formic acid.⁷

In a recent work, McQuigg and Calvert⁸ studied the photodecomposition of formaldehyde by flash photolysis. Two distinct primary photodissociative processes have been found in the photolysis of formaldehyde. The authors found that the relative quantum efficiencies of the two processes show a marked dependence on the wavelength of absorbed light. From this work and others,⁹ it is concluded that the upper limit of $D_{\rm HCO-H}$ is 81.5–85 kcal/mol.

Prior to the present work, the formyl radical has not been obtained via energy transfer from a donor to formaldehyde. In addition, the present work discusses

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the reactions in terms of (1) the monophotonic vs. the biphotonic dependence upon the nature of the solvent, (2) the concentration and temperature dependence, (3) the nature and role of donor and solvent radicals, and (4) the mechanisms.

Experimental Section

Purified paraformaldehyde from Fisher Scientific Co. that had been dryed 2 days in a vacuum desiccator over sulfuric acid was used. Formaldehyde was prepared in either of two ways. Formaldehyde gas formed from the decomposition of paraformaldehyde in mineral oil (at 120–140°) was passed through a CaCl₂ tube, together with nitrogen as carrier, directly into the appropriate solvent. The other method followed that described by Spence and Wild.¹⁰

Phillips Petroleum Co. pure grade 3-methylpentane (3-MP) was distilled of Na-Pb alloy and passed over dryed neutral silica gel and then over a silica gel-silver nitrate column. Fisher methylene chloride (reagent grade) and pure Eastman Organic Chemicals Co. triphenylamine (TPA) were used without further purification.

For photoreactions of TPA on silica gel, the experiment was conducted as follows: 12 mg of TPA in 5 ml of 3-MP was added to 1 g of silica gel; the mixture was evaporated and dried under vacuum for 1 day. From this was taken 0.4 g and formaldehyde was distilled onto the mixture as described in the literature.¹¹ Solutions of TPA and formaldehyde were obtained as follows: in an esr sample tube, 0.4 ml of a solution of TPA (2.5 mg in 1 cc of 3-MP) was added, the solvent vacuum evaporated, and formaldehyde distilled onto the TPA.

Solutions of formaldehyde in high concentrations (>5 \times 10⁻² M) in 3-MP are not stable at room temperature.¹¹ For this reason, cooling needs to be done very quickly for reproducible results.

Absorption spectra were taken on a Cary 15 recording spectrophotometer. The emission spectra were determined by the frontface method as described by Becker, *et al.*¹² Epr determinations were conducted in a Varian (E-3) epr spectrometer, and all irradiations were conducted with a 100-W high-pressure mercury lamp.

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